MATH 0030 Introduction to Calculus Lab
Lab for Math 103
Corequisite: MATH 1300
0 Course Units

MATH 0040 Calculus Lab I
Lab for Math 1400
Corequisite: MATH 1400
0 Course Units

MATH 0100 Calculus for Wharton Students Lab
Lab for Math 110
Fall
Corequisite: MATH 1100
0 Course Units

MATH 0140 Calculus II Lab
Lab for Math 114
Corequisite: MATH 1410
0 Course Units

MATH 0240 Calculus III Lab
Lab for Math 240
Corequisite: MATH 2400
0 Course Units

MATH 1070 Mathematics of change, Part I
Limits, orders of magnitude, differential and integral calculus;
Taylor polynomials; estimating and bounding; probability densities.
Mathematical modeling and applications to the social, economic and
information sciences.
1 Course Unit

MATH 1080 Mathematics of change, Part II
Multivariate calculus; optimization; multivariate probability densities.
Introduction to linear algebra; introduction to differential equations.
Mathematical modeling and applications to the social, economic and
information sciences.
1 Course Unit

MATH 1100 Calculus for Wharton Students
Differential calculus, integral calculus, series, differential equations and
elements of multivariable calculus, with an emphasis on applications.
Fall or Spring
Mutually Exclusive: MATH 1400
1 Course Unit

MATH 1234 Community Algebra Initiative
Community Algebra Initiative
Fall or Spring
1 Course Unit

MATH 1248 Community Math Teaching Project
This course allows Penn students to teach a series of hands-on activities
to students in math classes at University City High School. The semester
starts with an introduction to successful approaches for teaching math
in urban high schools. The rest of the semester will be devoted to a series
of weekly hands-on activities designed to teach fundamental aspects
of geometry. The first class meeting of each week, Penn faculty teach
Penn students the relevant mathematical background and techniques
for a hands-on activity. During the second session of each week, Penn
students will teach the hands-on activity to a small group of UCHS
students. The Penn students will also have an opportunity to develop
their own activity and to implement it with the UCHS students.
Not Offered Every Year
1 Course Unit

MATH 1400 Calculus, Part I
Brief review of High School calculus, applications of integrals,
transcendental functions, methods of integration, infinite series, Taylor's
theorem, and first order ordinary differential equations. Use of symbolic
manipulation and graphics software in calculus.
Fall or Spring
Mutually Exclusive: MATH 1100
1 Course Unit

MATH 1410 Calculus, Part II
Functions of several variables, vector-valued functions, partial
derivatives and applications, double and triple integrals, conic sections,
polar coordinates, vectors and vector calculus, first order ordinary
differential equations. Applications to physical sciences. Use of symbolic
manipulation and graphics software in calculus.
Fall or Spring
Mutually Exclusive: MATH 1510
Prerequisite: MATH 1400
1 Course Unit

MATH 1510 Calculus, Part II with Probability and Matrices
Functions of several variables, partial derivatives and applications, double and triple integrals, conic sections,
polar coordinates, vectors and vector calculus, first order ordinary
differential equations. Applications to physical sciences. Use of symbolic
manipulation and graphics software in calculus.
Fall or Spring
Mutually Exclusive: MATH 1400, MATH 1610
Prerequisite: MATH 1400
1 Course Unit

MATH 1610 Honors Calculus
Students who are interested in math or science might also want to
consider a more challenging Honors version of Calculus II and III, Math
1610 and Math 2600 (the analogues of Math 1410 and Math 2400,
respectively). These courses will cover essentially the same material
as 1610 and 2400, but more in depth and involve discussion of the
underlying theory as well as computations.
Fall or Spring
Mutually Exclusive: MATH 1510
1 Course Unit

MATH 1700 Ideas in Mathematics
Topics from among the following: logic, sets, calculus, probability,
history and philosophy of mathematics, game theory, geometry, and their
relevance to contemporary science and society.
Fall or Spring
1 Course Unit
MATH 2020 Proving Things: Analysis
This course focuses on the creative side of mathematics, with an emphasis on discovery, reasoning, proofs and effective communication, while at the same time studying real and complex numbers, sequences, series, continuity, differentiability and integrability. Small class sizes permit an informal, discussion-type atmosphere, and often the entire class works together on a given problem. Homework is intended to be thought-provoking, rather than skill-sharpening.
Fall or Spring
Prerequisite: MATH 1400 OR MATH 1410 OR MATH 2400
1 Course Unit

MATH 2030 Proving things: Algebra
This course focuses on the creative side of mathematics, with an emphasis on discovery, reasoning, proofs and effective communication, while at the same time studying arithmetic, algebra, linear algebra, groups, rings and fields. Small class sizes permit an informal, discussion-type atmosphere, and often the entire class works together on a given problem. Homework is intended to be thought-provoking, rather than skill-sharpening.
Fall or Spring
Prerequisite: MATH 1400 OR MATH 1410 OR MATH 2400
1 Course Unit

MATH 2100 Mathematics in the Age of Information
This course counts as a regular elective for both the Mathematics Major and Minor. This is a course about mathematical reasoning and the media. Embedded in many stories one finds in the media are mathematical questions as well as implicit mathematical models for how the world behaves. We will discuss ways to recognize such questions and models, and how to think about them from a mathematical perspective. A key part of the course will be about what constitutes a mathematical proof, and what passes for proof in various media contexts. The course will cover a variety of topics in logic, probability and statistics as well as how these subjects can be used and abused.
Fall or Spring
Prerequisite: MATH 1410 OR MATH 1510
1 Course Unit

MATH 2400 Calculus, Part III
Linear algebra: vectors, matrices, systems of linear equations, vector spaces, subspaces, spans, bases, and dimension, eigenvalues, and eigenvectors, matrix exponentials. Ordinary differential equations: higher-order homogeneous and inhomogeneous ODEs and linear systems of ODEs, phase plane analysis, non-linear systems.
Fall or Spring
Prerequisite: MATH 1410
1 Course Unit

MATH 2410 Calculus, Part IV
Partial differential equations and their solutions, including solutions of the wave, heat and Laplace equations, and Sturm-Liouville problems. Introduction to Fourier series and Fourier transforms. Computation of solutions, modeling using PDE’s, geometric intuition, and qualitative understanding of the evolution of systems according to the type of partial differential operator.
Fall or Spring
Prerequisite: MATH 2400
1 Course Unit

MATH 2500 Honors Calculus, Part II
This is an honors version of Math 2400 which explores the same topics but with greater mathematical rigor.
Not Offered Every Year
Prerequisite: MATH 1410
1 Course Unit

MATH 2800 Entropy Math Evolution
The goal of this is to explore a new theory of evolution developed by L. Demetrius at MIT based on the second law of thermodynamics. The essential idea is that life exists because it increases overall entropy quicker than other processes. The course will include an introduction to thermodynamics as well as to the information theory definition of entropy. Eventually I want to apply this to other systems. For instance, I think the theory explains why political candidates who create chaos, tweet and require more bits of information to describe each day are favored by the second law. Demetrius makes a distinction between robust high entropy environments and precarious low entropy environments which is very interesting in many different systems.
Fall
1 Course Unit

MATH 2900 Undergraduate Mathematics Research Course
This is a project-oriented mathematics research course that teaches students to solve real-world problems by constructing and analyzing mathematical models. Typically the problems considered will come from mathematics, chemistry, biology, and materials science but sometimes they will also come from economics, finance, and social sciences. The research problems in the course vary from year to year.
1 Course Unit

MATH 2989 Study Abroad
Free elective for undergraduate mathematics courses not equivalent to existing courses satisfying math major requirements.
1 Course Unit

MATH 2990 Undergraduate Research in Mathematics
Research conducted with the supervision of a faculty member. Must be approved by the Undergraduate Chair. May be repeated for credit.
Spring
1 Course Unit

MATH 2999 Transfer and Credit Away
Free elective for undergraduate mathematics courses not equivalent to existing courses satisfying math major requirements.
1 Course Unit

MATH 3120 Linear Algebra
Linear transformations, Gauss Jordan elimination, eigenvalues and eigenvectors, theory and applications. Mathematics majors are advised that MATH 3120 cannot be taken to satisfy the major requirements.
Not Offered Every Year
Prerequisite: MATH 2400
1 Course Unit
MATH 3130 Computational Linear Algebra
Many important problems in a wide range of disciplines within computer science and throughout science are solved using techniques from linear algebra. This course will introduce students to some of the most widely used algorithms and illustrate how they are actually used. Some specific topics: the solution of systems of linear equations by Gaussian elimination, dimension of a linear space, inner product, cross product, change of basis, affine and rigid motions, eigenvalues and eigenvectors, diagonalization of both symmetric and non-symmetric matrices, quadratic polynomials, and least squares optimization. Applications will include the use of matrix computations to computer graphics, use of the discrete Fourier transform and related techniques in digital signal processing, the analysis of systems of linear differential equations, and singular value decompositions with application to a principal component analysis. The ideas and tools provided by this course will be useful to students who intend to tackle higher level courses in digital signal processing, computer vision, robotics, and computer graphics.
Prerequisite: MATH 2400
1 Course Unit

MATH 3140 Advanced Linear Algebra
Topics will include: Vector spaces, Basis and dimension, quotients; Linear maps and matrices; Determinants, Dual spaces and maps; Invariant subspaces, Canonical forms; Scalar products: Euclidean, unitary and symplectic spaces; Orthogonal and Unitary operators; Tensor products and polyninear maps; Symmetric and skew-symmetric tensors and exterior algebra.
Prerequisite: MATH 2400
1 Course Unit

MATH 3200 Computer Methods in Mathematical Science I
Students will use symbolic manipulation software and write programs to solve problems in numerical quadrature, equation-solving, linear algebra and differential equations. Theoretical and computational aspects of the methods will be discussed along with error analysis and a critical comparison of methods.
Fall
Prerequisite: MATH 2400
1 Course Unit

MATH 3400 Discrete Mathematics I
Topics will be drawn from some subjects in combinatorial analysis with applications to many other branches of math and science: graphs and networks, generating functions, permutations, posets, asymptotics. Not Offered Every Year
Also Offered As: LGIC 2100
Prerequisite: MATH 1410 OR MATH 1510
1 Course Unit

MATH 3410 Discrete Mathematics II
Topics will be drawn from some subjects useful in the analysis of information and computation: logic, set theory, theory of computation, number theory, probability, and basic cryptography.
Also Offered As: LGIC 2200
Prerequisite: MATH 3400
1 Course Unit

MATH 3500 Number Theory
Congruences, Diophantine equations, continued fractions, nonlinear congruences, and quadratic residues.
Not Offered Every Year
1 Course Unit

MATH 3600 Advanced Calculus
Syllabus for MATH 360-361: a study of the foundations of the differential and integral calculus, including the real numbers and elementary topology, continuous and differentiable functions, uniform convergence of series of functions, and inverse and implicit function theorems. MATH 508-509 is a masters level version of this course.
Fall or Spring
Prerequisite: MATH 2400
1 Course Unit

MATH 3610 Advanced Calculus
Continuation of MATH 3600.
Fall or Spring
Prerequisite: MATH 3600
1 Course Unit

MATH 3700 Algebra
Syllabus for MATH 370-371: an introduction to the basic concepts of modern algebra. Linear algebra, eigenvalues and eigenvectors of matrices, groups, rings and fields. MATH 502-503 is a masters level version of this course.
Fall or Spring
Prerequisite: MATH 2400 OR MATH 2600
1 Course Unit

MATH 3710 Algebra
Continuation of MATH 3700.
Fall or Spring
Prerequisite: MATH 3700 OR MATH 5020
1 Course Unit

MATH 4100 Complex Analysis
Complex numbers, DeMoivre's theorem, complex valued functions of a complex variable, the derivative, analytic functions, the Cauchy-Riemann equations, complex integration, Cauchy's integral theorem, residues, computation of definite integrals by residues, and elementary conformal mapping.
Fall or Spring
Prerequisite: MATH 2400
1 Course Unit

MATH 4200 Ordinary Differential Equations
After a rapid review of the basic techniques for solving equations, the course will discuss one or more of the following topics: stability of linear and nonlinear systems, boundary value problems and orthogonal functions, numerical techniques, Laplace transform methods.
Fall or Spring
Prerequisite: MATH 2400
1 Course Unit

MATH 4250 Partial Differential Equations
Method of separation of variables will be applied to solve the wave, heat, and Laplace equations. In addition, one or more of the following topics will be covered: qualitative properties of solutions of various equations (characteristics, maximum principles, uniqueness theorems), Laplace and Fourier transform methods, and approximation techniques.
Fall
Prerequisite: MATH 2400
1 Course Unit
MATH 4320 Game Theory.
A mathematical approach to game theory, with an emphasis on examples of actual games. Topics will include mathematical models of games, combinatorial games, two person (zero sum and general sum) games, non-cooperating games and equilibria.
Fall or Spring
Prerequisite: MATH 2400
1 Course Unit

MATH 4600 Topology
Point set topology: metric spaces and topological spaces, compactness, connectedness, continuity, extension theorems, separation axioms, quotient spaces, topologies on function spaces, Tychonoff theorem. Fundamental groups and covering spaces, and related topics.
Not Offered Every Year
Prerequisite: MATH 2400 AND MATH 2410
1 Course Unit

MATH 4650 Differential Geometry
Differential geometry of curves in the plane and in 3-space; n gauge theories. Surfaces in 3-space; The geometry of the Gauss map; ons. The language of Intrinsic geometry of surfaces; Geodesics; Moving frames; of vector bundles, The Gauss-Bonnet Theorem; Assorted additional topics.
Not Offered Every Year
Prerequisite: (MATH 2400 OR MATH 2600) AND (MATH 3140 OR MATH 5140)
1 Course Unit

MATH 4800 Topics in Modern Math
Mathematics 4800 will open with a review of the basics of real analysis (brief or extended background requires). The review will include: introduction of the real numbers through Dedekind cuts, continuity of real-valued functions on the real line; Cantor nested-interval principle, basic results for continuous functions, Maximum and Intermediate Value theorems, Heine-Borel Theorem, Uniform Continuity on closed intervals; metric spaces, convergence of sequences, Cauchy sequences, completeness, more general uniform continuity and intermediate value theorems; general topology, separation, compactness, product spaces, Tychonoff's Theorem. Special topics in analysis: Weierstrass Polynomial Approximation Theorem, Bernstein polynomials and simultaneous approxfunctions and derivatives, topics from divergent series, summation methods; r measure theory, the Lebesgue integral, Lp spaces, Holder, Minkowski, and and Cauchy-Schwarz inequalities; basics of Functional Analysis, normed spaces, Banach spaces and Hilbert space, with examples (Lp spaces, continuous-functions spaces), Banach spaces and spectral theory, groups and Fourier transforms, Tauberian theorems; approximation theory, again, through the prism of functional analysis; extension of the polynomial approximation theorem (Stone-Weierstrass theorem), Muntz approximation theorem (by polynomials with preassigned powers), compact operators, the Spectral theorem, Stone's theorem (representations of the additive group of real numbers); Peter-Weyl theory (representations of compact groups). A selection from these topics as time and class preparation allow.
Not Offered Every Year
Prerequisite: MATH 2400 OR MATH 2600) AND (MATH 3140 OR MATH 5140)
1 Course Unit

MATH 4990 Supervised Study
Study under the direction of a faculty member. Intended for a limited number of mathematics majors.
Fall or Spring
1 Course Unit
MATH 5080 Advanced Analysis
Construction of real numbers, the topology of the real line and the foundations of single variable calculus. Notions of convergence for sequences of functions. Basic approximation theorems for continuous functions and rigorous treatment of elementary transcendental functions. The course is intended to teach students how to read and construct rigorous formal proofs. A more theoretical course than Math 3600.
Fall
Prerequisite: MATH 2400 AND MATH 2410
1 Course Unit

MATH 5090 Advanced Analysis
Spring
Prerequisite: MATH 5080
1 Course Unit

MATH 5120 Advanced Linear Algebra
Topics will include: Vector spaces, Basis and dimension, quotients; Linear maps and matrices; Determinants, Dual spaces and maps; Invariant subspaces, Cononical forms; Scalar products: Euclidean, unitary and symplectic spaces; Orthogonal and unitary operators; Tensor products and polylinear maps; Symmetric and skew-symmetric tensors and exterior algebra.
1 Course Unit

MATH 5130 Computational Linear Algebra
A number of important and interesting problems in a wide range of disciplines within computer science are solved by recourse to techniques from linear algebra. The goal of this course will be to introduce students to some of the most important and widely used algorithms in matrix computation and to illustrate how they are actually used in various settings. Motivating applications will include: the solution of systems of linear equations, applications matrix computations to modeling geometric transformations in graphics, applications of the Discrete Fourier Transform and related techniques in digital signal processing, the solution of linear least squares optimization problems and the analysis of systems of linear differential equations. The course will cover the theoretical underpinnings of these problems and the numerical algorithms that are used to perform important matrixcomputations such as Gaussian Elimination, LU Decomposition and Singular Value Decomposition.
Prerequisite: MATH 2400
1 Course Unit

MATH 5140 Advanced Linear Algebra
Topics will include: Vector spaces, Basis and dimension, quotients; Linear maps and matrices; Determinants, Dual spaces and maps; Invariant subspaces, Cononical forms; Scalar products: Euclidean, unitary and symplectic spaces; Orthogonal and Unitary operators; Tensor products and polylinear maps; Symmetric and skew-symmetric tensors and exterior algebra.
Also Offered As: AMCS 5141
Prerequisite: MATH 2400
1 Course Unit

MATH 5200 Selections from Algebra
Informal introduction to such subjects as homological algebra, number theory, and algebraic geometry.
Not Offered Every Year
Prerequisite: MATH 5020
Corequisite: MATH 5020
1 Course Unit

MATH 5300 Mathematics of Finance
This course presents the basic mathematical tools to model financial markets and to make calculations about financial products, especially financial derivatives. Mathematical topics covered: stochastic processes, partial differential equations and their relationship. No background in finance is assumed.
Not Offered Every Year
Prerequisite: MATH 2400 OR MATH 2600 STAT 4300
1 Course Unit

MATH 5400 Selections from Classical and Functional Analysis
Informal introduction to such subjects as compact operators and Fredholm theory, Banach algebras, harmonic analysis, differential equations, nonlinear functional analysis, and Riemann surfaces.
Not Offered Every Year
1 Course Unit

MATH 5460 Advanced Applied Probability
The required background is (1) enough math background to understand proof techniques in real analysis (closed sets, uniform convergence, fourier series, etc.) and (2) some exposure to probability theory at an intuitive level (a course at the level of Ross's probability text or some exposure to probability in a statistics class).
Fall
Also Offered As: AMCS 5461
1 Course Unit

MATH 5500 Selections from Geometry and Topology
Informal introduction to such subjects as homology and homotopy theory, classical differential geometry, dynamical systems, and knot theory.
Not Offered Every Year
Prerequisite: MATH 5000
Corequisite: MATH 5000
1 Course Unit

MATH 5600 Selections from Geometry and Topology
Informal introduction to such subjects as homology and homotopy theory, classical differential geometry, dynamical systems, and knot theory.
Not Offered Every Year
Prerequisite: MATH 5000
Corequisite: MATH 5000
1 Course Unit

MATH 5610 Selections from Geometry and Topology
Informal introduction to such subjects as homology and homotopy theory, classical differential geometry, dynamical systems, and knot theory.
Not Offered Every Year
Prerequisite: MATH 5000
Corequisite: MATH 5000
1 Course Unit

MATH 5700 Logic and Computability 1
The course focuses on topics drawn from the central areas of mathematical logic: model theory, proof theory, set theory, and computability theory.
Not Offered Every Year
Also Offered As: PHIL 6721
Prerequisite: MATH 3710 OR MATH 5030
1 Course Unit
MATH 5710 Logic and Computability 2
A continuation of PHIL 6721.
Not Offered Every Year
Also Offered As: PHIL 6722
Prerequisite: MATH 5700
1 Course Unit

MATH 5800 Combinatorial Analysis
Standard tools of enumerative combinatorics including partitions and compositions of integers, set partitions, generating functions, permutations with restricted positions, inclusion-exclusion, partially ordered sets. Permission of the instructor required to enroll.
Not Offered Every Year
1 Course Unit

MATH 5810 Topics in Combinatorial Theory
Variable topics connected to current research in combinatorial theory. Recent topics include algebraic combinatorics and symmetric functions, analytic combinatorics and discrete probability.
Not Offered Every Year
Prerequisite: MATH 5800
1 Course Unit

MATH 5840 The Mathematics of Medical Imaging and Measurement
The last several decades have seen major revolutions in both medical and non-medical and imaging technologies. Underlying all of these advances are sophisticated mathematical tools to model the measurement process and reconstruct images. This course begins with an introduction of the mathematical models and then proceeds to discuss the integral transforms that underlie these models: the Fourier transform, the Radon transform and the Laplace transform. We discuss how each of these transforms is inverted, both in theory and in practice. Along the way we study interpolation, sampling, approximation theory, filtering and noise analysis. This course assumes a thorough knowledge of linear algebra and a knowledge of analysis at the undergraduate level (MATH 3140 and MATH 3600 and MATH 3610, or MATH 5080 and MATH 5090).
Not Offered Every Year
Also Offered As: AMCS 5840, BE 5840
Prerequisite: MATH 1410 AND (MATH 3600 OR MATH 5080) AND (MATH 3610 OR MATH 5090)
1 Course Unit

MATH 5861 Mathematical Modeling in Biology
This course will cover various mathematical models and tools that are used to study modern biological problems. Mathematical models may be drawn from cell biology, physiology, population genetics, or ecology. Tools in dynamical systems or stochastic processes will be introduced as necessary. No prior knowledge of biology is needed to take this course, but some familiarity with differential equations and probability will be assumed.
Fall
Also Offered As: BIOL 5860
1 Course Unit

MATH 5940 Mathematical Methods of Physics
A discussion of those concepts and techniques of classical analysis employed in physical theories. Topics include complex analysis, Fourier series and transforms, ordinary and partial equations, Hilbert spaces, among others.
Fall
Also Offered As: PHYS 5500
1 Course Unit

MATH 5999 Independent Study
Study under the direction of a faculty member. Hours to be arranged.
Fall or Spring
1-4 Course Units

MATH 6000 Topology and Geometric Analysis
Differentiable functions, inverse and implicit function theorems. Theory of manifolds: differentiable manifolds, charts, tangent bundles, transversality, Sard’s theorem, vector and tensor fields and differential forms: Frobenius’ theorem, integration on manifolds, Stokes’ theorem in n dimensions, de Rham cohomology. Introduction to Lie groups and Lie group actions.
Fall
Prerequisite: MATH 5000 AND MATH 5010
1 Course Unit

MATH 6020 Algebra
Fall
Prerequisite: (MATH 3700 AND MATH 3710) OR (MATH 5020 AND MATH 5030)
1 Course Unit

MATH 6030 Algebra
Continuation of Math 6020.
Spring
Prerequisite: MATH 6020
1 Course Unit

MATH 6040 First Year Seminar in Mathematics
This is a seminar for first year Mathematics graduate students, supervised by faculty. Students give talks on topics from all areas of mathematics at a level appropriate for first year graduate students. Attendance and preparation will be expected by all participants, and learning how to present mathematics effectively is an important part of the seminar.
Fall
1 Course Unit
MATH 6080 Analysis
Complex analysis: analyticity, Cauchy theory, meromorphic functions, isolated singularities, analytic continuation, Runge's theorem, d-bar equation, Mittag-Leffler theorem, harmonic and sub-harmonic functions, Riemann mapping theorem, Fourier transform from the analytic perspective. Introduction to real analysis: Weierstrass approximation, Lebesgue measure in Euclidean spaces, Borel measures and convergence theorems, $C_0$ and the Riesz-Markov theorem, $L_p$-spaces, Fubini Theorem. Fall or Spring
Also Offered As: AMCS 6081
Prerequisite: MATH 5080 AND MATH 5090
1 Course Unit

MATH 6090 Analysis
Real analysis: general measure theory, outer measures and Cartheodory construction, Hausdorff measures, Radon-Nikodym theorem, Fubini's theorem, Hilbert space and $L^2$-theory of the Fourier transform. Functional analysis: normed linear spaces, convexity, the Hahn-Banach theorem, duality for Banach spaces, weak convergence, bounded linear operators, Baire category theorem, uniform boundedness principle, open mapping theorem, closed graph theorem, compact operators, Fredholm theory. Fall or Spring
Also Offered As: AMCS 6091
Prerequisite: MATH 6080
1 Course Unit

MATH 6100 Functional Analysis
Prerequisite: MATH 6080 OR MATH 6090
1 Course Unit

MATH 6120 Selections from Algebra
Informal introduction to such subjects as homological algebra, number theory, and algebraic geometry.
Not Offered Every Year
Prerequisite: MATH 6000 AND MATH 6020
Corequisites: MATH 6000, MATH 6020
1 Course Unit

MATH 6180 Algebraic Topology, Part I
Fall
Prerequisite: MATH 6000 AND MATH 6010
1 Course Unit

MATH 6190 Algebraic Topology, Part I
Rational homotopy theory, cobordism, K-theory, Morse theory and the h-cobordism theorem. Surgery theory.
Spring
Prerequisite: MATH 6180
1 Course Unit

MATH 6200 Algebraic Number Theory
Dedekind domains, local fields, basic ramification theory, product formula, Dirichlet unit theory, finiteness of class numbers, Hensel's Lemma, quadratic and cyclotomic fields, quadratic reciprocity, abelian extensions, zeta and $L$-functions, functional equations, introduction to local and global class field theory. Other topics may include: Diophantine equations, continued fractions, approximation of irrational numbers by rationals, Poisson summation, Hasse principle for binary quadratic forms, modular functions and forms, theta functions.
Not Offered Every Year
Prerequisite: MATH 6020 AND MATH 6030
1 Course Unit

MATH 6210 Algebraic Number Theory
Continuation of Math 6200.
Not Offered Every Year
Prerequisite: MATH 6200
1 Course Unit

MATH 6220 Complex Algebraic Geometry
Algebraic geometry over the complex numbers, using ideas from topology, complex variable theory, and differential geometry. Topics include: Complex algebraic varieties, cohomology theories, line bundles, vanishing theorems, Riemann surfaces, $A^1$-affine theorem, linear systems, complex tori and abelian varieties, Jacobian varieties, currents, algebraic surfaces, adjunction formula, rational surfaces, residues.
Not Offered Every Year
Prerequisite: MATH 6020 AND MATH 6030 AND MATH 6090
1 Course Unit

MATH 6230 Complex Algebraic Geometry
Continuation of Math 6220.
Not Offered Every Year
Prerequisite: MATH 6220
1 Course Unit

MATH 6240 Algebraic Geometry
Algebraic geometry over algebraically closed fields, using ideas from commutative algebra. Topics include: Affine and projective algebraic varieties, morphisms and rational maps, singularities and blowing up, rings of functions, algebraic curves, Riemann Roch theorem, elliptic curves, Jacobian varieties, sheaves, schemes, divisors, line bundles, cohomology of varieties, classification of surfaces.
Not Offered Every Year
Prerequisite: MATH 6020 AND MATH 6030
1 Course Unit

MATH 6250 Algebraic Geometry
Continuation of Math 6240.
Not Offered Every Year
Prerequisite: MATH 6240
1 Course Unit

MATH 6260 Commutative Algebra
Topics in commutative algebra taken from the literature. Material will vary from year to year depending upon the instructor's interests.
Not Offered Every Year
Prerequisite: MATH 6020 AND MATH 6030
1 Course Unit
MATH 6280 Homological Algebra
Complexes and exact sequences, homology, categories, derived functors (especially Ext and Tor). Homology and cohomology arising from complexes in algebra and geometry, e.g. simplicial and singular theories, Cech cohomology, de Rham cohomology, group cohomology, Hochschuld cohomology. Projective resolutions, cohomological dimension, derived categories, spectral sequences. Other topics may include: Lie algebra cohomology, Galois and etale cohomology, cyclic cohomology, l-adic cohomology. Algebraic deformation theory, quantum groups, Brauer groups, descent theory.
Not Offered Every Year
Prerequisite: MATH 6020 AND MATH 6030
1 Course Unit

MATH 6290 Homological Algebra
Continuation of Math 6280.
Not Offered Every Year
Prerequisite: MATH 6280
1 Course Unit

MATH 6340 Arithmetic Geometry
Arithmetic Geometry
1 Course Unit

MATH 6420 Topics in Partial Differential Equations
Problems in differential geometry, as well as those in physics and engineering, inevitably involve partial derivatives. This course will be an introduction to these problems and techniques. We will use P.D.E. as a tool. Some of the applications will be small, some large. The proof of the Hodge Theorem will be a small application. Discussion of the Yamabe problem and Ricci flow (used to prove the Poincare Conjecture) will be larger.
Prerequisite: MATH 6080 AND MATH 6090
1 Course Unit

MATH 6440 Partial Differential Equations
Subject matter varies from year to year. Some topics are: the classical theory of the wave and Laplace equations, general hyperbolic and elliptic equations, theory of equations with constant coefficients, pseudo-differential operators, and non-linear problems. Sobolev spaces and the theory of distributions will be developed as needed.
Not Offered Every Year
Prerequisite: MATH 6080 AND MATH 6090
1 Course Unit

MATH 6450 Partial Differential Equations
Subject matter varies from year to year. Some topics are: the classical theory of the wave and Laplace equations, general hyperbolic and elliptic equations, theory of equations with constant coefficients, pseudo-differential operators, and non-linear problems. Sobolev spaces and the theory of distributions will be developed as needed.
Not Offered Every Year
Prerequisite: MATH 6080 AND MATH 6090
1 Course Unit

MATH 6480 Probability Theory
Measure theoretic foundations, laws of large numbers, large deviations, distributional limit theorems, Poisson processes, random walks, stopping times.
Fall
Also Offered As: AMCS 6481, STAT 9300
Prerequisite: STAT 4300 OR STAT 5100 OR MATH 6080
1 Course Unit

MATH 6490 Stochastic Processes
Continuation of MATH 6480/STAT 9300, the 2nd part of Probability Theory for PhD students in the math or statistics department. The main topics include Brownian motion, martingales, Ito's formula, and their applications to random walk and PDE.
Not Offered Every Year
Also Offered As: AMCS 6491, STAT 9310
1 Course Unit

MATH 6520 Operator Theory
Subject matter may include spectral theory of operators in Hilbert space, C*-algebras, von Neumann algebras.
Not Offered Every Year
1 Course Unit

MATH 6540 Lie Groups
Connection of Lie groups with Lie algebras, Lie subgroups, exponential map. Algebraic Lie groups, compact and complex Lie groups, solvable and nilpotent groups. Other topics may include relations with symplectic geometry, the orbit method, moment map, symplectic reduction, geometric quantization, Poisson-Lie and quantum groups.
Not Offered Every Year
Prerequisite: MATH 6000 AND MATH 6010 AND MATH 6020 AND MATH 6030
1 Course Unit

MATH 6550 Lie Groups
Continuation of Math 6540.
Not Offered Every Year
Prerequisite: MATH 6540
1 Course Unit

MATH 6560 Representation of Continuous Groups
Possible topics: harmonic analysis on locally compact abelian groups; almost periodic functions; direct integral decomposition theory, Types I, II and III: induced representations, representation theory of semisimple groups.
Not Offered Every Year
1 Course Unit

MATH 6600 Differential Geometry
Riemannian metrics and connections, geodesics, completeness, Hopf-Rinow theorem, sectional curvature, Ricci curvature, scalar curvature, Jacobi fields, second fundamental form and Gauss equations, manifolds of constant curvature, first and second variation formulas, Bonnet-Myers theorem, comparison theorems, Morse index theorem, Hadamard theorem, Preissmann theorem, and further topics such as sphere theorems, critical points of distance functions, the soul theorem, Gromov-Hausdorff convergence.
Not Offered Every Year
Prerequisite: MATH 6000 AND 6010 AND 6020 AND 6030
1 Course Unit

MATH 6610 Differential Geometry
Continuation of Math 6600.
Not Offered Every Year
Prerequisite: MATH 6600
1 Course Unit

MATH 6610 Differential Geometry
Continuation of Math 6600.
Not Offered Every Year
Prerequisite: MATH 6600
1 Course Unit

MATH 6710 Topics in Logic
Discusses advanced topics in logic.
Not Offered Every Year
Prerequisite: MATH 5700 AND MATH 5710
1 Course Unit
MATH 6770 Topics in Logic
This graduate course focuses on topics drawn from the central areas of mathematical logic: model theory, proof theory, set theory, and computability theory.
Not Offered Every Year
Also Offered As: PHIL 6720
1 Course Unit

MATH 6940 Mathematical Foundations of Theoretical Physics
Selected topics in mathematical physics, such as mathematical methods of classical mechanics, electrodynamics, relativity, quantum mechanics and quantum field theory.
Not Offered Every Year
1 Course Unit

MATH 6950 Mathematical Foundations of Theoretical Physics
Selected topics in mathematical physics, such as mathematical methods of classical mechanics, electrodynamics, relativity, quantum mechanics and quantum field theory.
Not Offered Every Year
1 Course Unit

MATH 6982 Representation of Continuous Groups
Possible topics: harmonic analysis on locally compact abelian groups; almost periodic functions; direct integral decomposition theory, Types I, II and III; induced representations, representation theory of semisimple groups.
Not Offered Every Year
1 Course Unit

MATH 7020 Topics in Algebra
Topics from the literature. The specific subjects will vary from year to year.
Not Offered Every Year
1 Course Unit

MATH 7200 Advanced Number Theory
Ramification theory, adeles and ideles, Tate’s thesis, group cohomology and Galois cohomology, class field theory in terms of ideles and cohomology, Lubin-Tate formal groups, Artin and Swan conductors, central simple algebras over local and global fields, general Hasse principles. Other topics may include the following: zero-dimensional Arakelov theory, Tate duality, introduction to arithmetic of elliptic curves, local and global epsilon factors in functional equations, p-adic L-functions and Iwasawa theory, modular forms and functions and modular curves.
Not Offered Every Year
Prerequisite: MATH 6200 AND MATH 6210
1 Course Unit

MATH 7210 Advanced Number Theory
Continuation of Math 7200.
Not Offered Every Year
Prerequisite: MATH 7200
1 Course Unit

MATH 7240 Topics in Algebraic Geometry
Topics from the literature. The specific subjects will vary from year to year.
Not Offered Every Year
Prerequisite: MATH 6220 AND (MATH 6230 OR MATH 6240) AND MATH 6250
1 Course Unit

MATH 7300 Topics in Algebraic and Differential Topology
Topics from the literature. The specific subjects will vary from year to year.
Not Offered Every Year
Prerequisite: MATH 6180 AND MATH 6190
1 Course Unit

MATH 7310 Topics in Algebraic and Differential Topology
Topics from the literature. The specific subjects will vary from year to year.
Not Offered Every Year
Prerequisite: MATH 6180 AND MATH 6190
1 Course Unit

MATH 7480 Topics in Classical Analysis
Harmonic analysis in Euclidean space, Riemann surfaces, Discontinuous groups and harmonic analysis in hyperbolic space, Pseudodifferential operators and index theorems, Variational methods in non-linear PDE, Hyperbolic equations and conservation laws, Probability and stochastic processes, Geometric measure theory, Applications of analysis to problems in differential geometry. The specific subjects will vary from year to year.
Not Offered Every Year
Prerequisite: MATH 6080 AND MATH 6090
1 Course Unit

MATH 7520 Topics in Operator theory
Topics from the literature. The specific subjects will vary from year to year.
Not Offered Every Year
1 Course Unit

MATH 7530 Topics in Operator Theory
Topics from the literature. The specific subjects will vary from year to year.
Not Offered Every Year
1 Course Unit

MATH 7600 Topics in Differential Geometry
Topics from the literature. The specific subjects will vary from year to year.
Not Offered Every Year
Prerequisite: MATH 6600 AND MATH 6610
1 Course Unit

MATH 7610 Topics in Differential Geometry
Topics from the literature. The specific subjects will vary from year to year.
Not Offered Every Year
Prerequisite: MATH 6600 AND MATH 6610
1 Course Unit

MATH 8200 Algebra Seminar
Seminar on current and recent literature in algebra.
Not Offered Every Year
1 Course Unit

MATH 8300 Geometry-Topology Seminar
Seminar on current and recent literature in geometry-topology
Not Offered Every Year
1 Course Unit

MATH 8310 Geometry-Topology Seminar
Seminar on current and recent literature in geometry-topology
Not Offered Every Year
1 Course Unit
MATH 8710 Logic Seminar
Seminar on current and recent literature in logic.
Not Offered Every Year
1 Course Unit

MATH 8780 Probability and Algorithm Seminar
Seminar on current and recent literature in probability and algorithms.
1 Course Unit

MATH 8810 Combinatorics Seminar
Seminar on current and recent literature in combinatorics.
Not Offered Every Year
1 Course Unit